

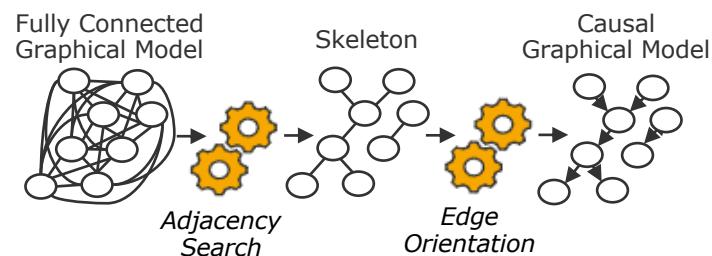
## Motivation

**Learning causal structures (CSL)** in high-dimensional data promises huge **potential in real-world applications**. CSL supports humans in **understanding highly complex systems** with abundant data and allows for a **causal interpretation**. For example, CSL provides data-driven decision support for effective troubleshooting in manufacturing<sup>[2]</sup>, or CSL supports genetic research when constructing gene regulatory networks to understand disease mechanisms. However, algorithms for constraint-based CSL have **high computational complexity** and are currently limited by their **long runtimes**.

➔ Enabling the **efficient execution** in **heterogeneous computing systems**, leveraging the parallel computing capabilities of Graphics Processing Units (GPUs) constitutes the **required speed-up for application in practice**.

## Background

One approach to CSL is constraint-based methods, which apply conditional independence (CI) tests suitable to the underlying data distribution of the observational data. Our work focuses on the PC algorithm<sup>[5]</sup> to learn the causal graphical model. The PC algorithm consists of two phases, see Fig. 1, with the adjacency search defining the overall computational complexity; thereby, it is the focus of our work.



**Fig. 1:** Sketch of the PC algorithm with its two phases to learn the causal graphical model from observational data

A GPU's parallel structure provides massive computational power and is well-suited for processing tasks exposing data parallelism. A GPU follows the SIMT execution model,

meaning that multiple threads execute the same instruction on different data. The data resides in the GPU's on-chip memory, which requires prior transfer from DRAM.

## Research Questions (RQ)

**(RQ1) How can we efficiently execute constraint-based CSL on a GPU, considering the SIMT execution model?** In this context, a parallel execution strategy and a definition of tasks for parallel execution are required, which need to reflect a suitable granularity. Further, the characteristics of various CI tests for different data distributions have to be considered.

**(RQ2) How can we scale constraint-based CSL on a GPU to very large datasets, which exceed the on-chip memory?** A data processing model is required in this context, which copes with the limited on-chip memory capacity and balances data transfer overhead.

**(RQ3) How can we fully utilize all processing units, e.g., CPUs and GPUs, in a heterogeneous computing system to jointly learn the causal structures?** In this context, load balancing mechanisms are required, which handle tasks for parallel execution with different granularities suitable for each processing unit.

## Contributions

### Development of `gpubcalc` - an R-package with C++/CUDA extensions

`gpubcalc` will include GPU-accelerated implementations of CI tests (*addressing RQ1*) for:

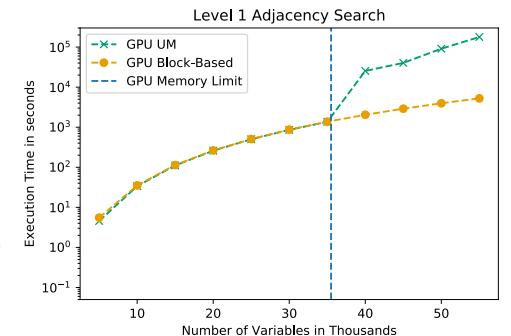
- multivariate normal distributed data<sup>[3]</sup>;
- discrete data<sup>[1]</sup>;
- and mixed data.

`gpubcalc` implements strategies (*addressing RQ2 & RQ3*) to:

- overcome single GPU memory limitations<sup>[4]</sup>;
- execute on multiple GPUs in parallel;
- and execute cooperatively on CPU-GPU.

## Preliminary Results

- On multivariate normal distributed data with limitation to conditioning sizes of up to 1 GPU-accelerated execution achieves **speed-up** over CPU-based execution of **factors up to 700**<sup>[3]</sup>.
- A block-based approach to overcome GPU memory limitations shows **improved scalability** over an implicit memory managed version Fig. 2<sup>[4]</sup>.
- On discrete data, GPU-accelerated execution achieves **speed-up** over CPU-based systems of **factors up to 62** Fig. 3<sup>[1]</sup>.
- Extension to multi-GPU promises reasonable **scaling with the number of devices** for multivariate normal distributed data.



**Fig. 2:** Comparing explicit (Block-Based) with implicit (UM) memory managed versions to scale CSL beyond GPU memory limitations

Dataset	parallelPC	bnlearn	disc-cupc	gpuPC
ALARM	579.54 s	14.71 s	0.95 s	0.26 s
ANDES	187.24 s	20.78 s	1.41 s	0.38 s
LINK	16,510.31 s	141.65 s	12.93 s	2.28 s
MUNIN	110,740.5 s	273.79 s	97.45 s	14.99 s

**Fig. 3:** Execution times of parallel adjacency searches within PC algorithm on discrete data on multi-core CPU (parallelPC, bnlearn) or GPU (disc-cupc, gpuPC)

## Conclusion

This thesis investigates parallel execution strategies within heterogeneous computing systems to efficiently execute CSL. While we achieve speed-up over conventional CPU-based approaches in several settings, it remains to define a generalized model for parallel execution of CSL based on CI test characteristics. Hence, our current effort is to extend our findings to other currently existing and future CI tests.

### References:

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- [5] Spirtes, P.;Glymour, C.;Scheines, R.:Causation, Prediction, and Search, Second Edition. Adaptive Computation and Machine Learning, MIT Press, Cambridge, MA, USA, 2000

- Note, some publications are published under my birth name Schmidt.